

Cambridge International AS & A Level

MATHEMATICS

Paper 5 Probability & Statistics 1 MARK SCHEME Maximum Mark: 50 9709/51 May/June 2022

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

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Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Mathematics	Specific	Marking	Principles
1.1	~~~~		

1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.	
2		

2 Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.

3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.

4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).

5 Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.

6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

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Mark Scheme Notes

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- **B** Mark for a correct result or statement independent of method marks.
- **DM** or **DB** When a part of a question has two or more 'method' steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
 - **FT** Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.
- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
- For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
- The total number of marks available for each question is shown at the bottom of the Marks column.
- Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
- Square brackets [] around text or numbers show extra information not needed for the mark to be awarded.

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Abbreviations

- AEF/OE Any Equivalent Form (of answer is equally acceptable) / Or Equivalent
- AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
- CAO Correct Answer Only (emphasising that no 'follow through' from a previous error is allowed)
- CWO Correct Working Only
- ISW Ignore Subsequent Working

- SC Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)
- WWW Without Wrong Working
- AWRT Answer Which Rounds To

SOI Seen Or Implied

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Question	Answer	Marks	Guidance
1(a)	5!	M1	k! where $k = 5, 6$ or 7 Condone $\times 1$ OE
	120	A1	
		2	
1(b)	[Total no of ways =] $\frac{8!}{2!3!}$ [= 3360]	M1	$\frac{8!}{a!b!}$, $a = 1,2$ $b = 1,3$ $a \neq b$
	[With 3Es together =] $\frac{6!}{2!}$ [= 360]	M1	$\frac{6!}{c!}$, $c = 1,2$ seen in an addition/subtraction
	[With 3Es not together] = 3360 - 360	M1	$\frac{8!}{d!e!} - \frac{6!}{f!}$ where $d, f = 1, 2 \& e = 1, 3$
	3000	A1	
		4	

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Question	Answer	Marks	Guidance
2(a)	$^{12}C_4 \times 2$	M1	${}^{g}C_{4} \times h$ $g = 12, 13, h = 1,2$
	990	A1	
	Alternative method for question 2(a)	· ·	
	$[\text{total} - \text{both on} - \text{neither on}]^{14}C_5 - (^{12}C_3 + ^{12}C_5) = [2002 - 220 - 792]$	M1	${}^{k}C_{5} - ({}^{a}C_{3} + {}^{a}C_{5})$ a = 12, 13 and k = 13, 14
	990	A1	
		2	
2(b)	$\begin{bmatrix} Mrs \ Lan \ plus \end{bmatrix} \\ 2W \ 2M {}^7C_2 \times {}^6C_2 = 315 \\ 3W \ 1M {}^7C_3 \times {}^6C_1 = 210 \\ 4W {}^7C_4 = 35 \end{bmatrix}$	M1	$^{7}C_{r} \times {}^{6}C_{4-r}$ for $r = 2, 3$ or 4
		B1	Outcome for one identifiable scenario correct, accept unevaluated
		M1	Add outcomes for 3 identifiable correct scenarios Note: if scenarios not labelled, they may be identified by seeing ⁷ C _r × ${}^{6}C_{s}r + s = 4$ to imply <i>r</i> women and <i>s</i> men for both B & M marks only
	[Total =] 560	A1	
		4	

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Question						Aı	Mark	s Guidance
3(a)	Class width Frequence density	20 cy 22	10 72	10 92	20 15	30 4	М	1 At least 4 frequency densities calculated (Frequency \div class width, e.g. $\frac{440}{20} \left(condone \frac{440}{19.5}, \frac{440}{20.5} \right)$ Accept unsimplified, may be read from graph using <i>their</i> scale
	t						A	1 All heights correct on graph NOT FT
	Frequency Density 90						В	1 Bar ends at $[0,]$ 20, 30, 40, 60, 90 at axis with a horizontal linear scale with at least 3 values indicated. $0 \leq$ horizontal scale ≤ 90
	50 50 50 30 20 10	10	20 30	40	50 60	- 70	В	Axes labelled frequency density (fd), time (t) and minutes (mins) or in a title. Linear vertical scale, with at least 3 values indicated 0 ≤ vertical axes ≤ 92 (condone 90 used).
								4

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Question	Answer	Marks	Guidance
3(b)	Midpoints 10 25 35 50 75	B1	At least 4 correct midpoints seen
	$\begin{bmatrix} Mean = 31.44 \text{ given} \end{bmatrix}$ $\begin{bmatrix} Variance = \frac{440 \times 10^2 + 720 \times 25^2 + 920 \times 35^2 + 300 \times 50^2 + 120 \times 75^2}{2500} - 31.44^2 \end{bmatrix}$ $= \frac{44000 + 450000 + 1127000 + 750000 + 675000}{2500} - 31.44^2$ $\begin{bmatrix} \frac{3046000}{2500} - 31.44^2 = 229.9264 \end{bmatrix}$ Or $Variance = \frac{440(10 - 31.44)^2 + 720(25 - 31.44)^2 + 920(35 - 31.44)^2 + 300(50 - 31.44)^2 + 120(75 - 31.44)^2}{2500}$ $= \frac{202256 + 29860 + 11659 + 103342 + 227697}{2500} = \frac{574814}{2500} = 229.9264$	M1	Correct formula for variance or standard deviation (– mean ² included with <i>their</i> midpoints (not upper bound, lower bound, class width, frequency density, frequency or cumulative frequency) and <i>their</i> \sum f if calculated. Condone 1 data error.
	Standard deviation = 15.2	A1	WWW, allow 15.16[3]
		3	
3(c)	30–40	B1	
		1	
3(d)	Stays the same, data still in same intervals	B1	Frequencies unchanged
		1	

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Question	Answer	Marks	Guidance
4(a)	$a = P(1 \text{ head}) = 0.7 \times (0.5)^3 + 0.3 \times (0.5)^3 \times 3 = \frac{1}{5}$	B1	Clear statement of unevaluated correct calculation $=\frac{1}{5}$. AG
	$b = 0.7 \times 0.5^{3} \times 3 + 0.3 \times 0.5^{3} \times 3 = \frac{3}{8}$ $c = 0.7 \times 0.5^{3} \times 3 + 0.3 \times 0.5^{3} = \frac{3}{10}$	M1	Clear statement of unevaluated calculation for either b or c
	$c = 0.7 \times 0.5^3 \times 3 + 0.3 \times 0.5^3 = \frac{3}{10}$	A1	For either b or c correct
	$\left[or c = \frac{27}{40} - b\right]$	B1 FT	$their b + their c = \frac{27}{40}$
		4	
4(b)	$\left[E(X) = \frac{3 \times 0 + 16 \times 1 + 30 \times 2 + 24 \times 3 + 7 \times 4}{80} = \right] \frac{176}{80} \text{ or } 2.2$	B1 FT	Correct or accept unsimplified calculation using <i>their</i> values for b and c seen (sum of probabilities = 1)
		1	

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Question	Answer	Marks	Guidance
4(c)	$[P(0, 1, 2) =]^{10}C_0 \ 0.2^0 \ 0.8^{10} \ + \ {}^{10}C_1 \ 0.2^1 \ 0.8^9 \ + \ {}^{10}C_2 \ 0.2^2 \ 0.8^8$	M1	One term ${}^{10}C_x p^x (1-p)^{10-x}$, for $0 < x < 10, 0 < p < 1$
	0.107374 + 0.268435 + 0.301989	A1	Correct expression, accept unsimplified leading to final answer
	0.678	B1	0.677
	Alternative method for question 4(c)		
	$\frac{1 - [{}^{10}C_{10} \ 0.2{}^{10}0.8^0 + {}^{10}C_9 \ 0.2{}^90.8^1 + {}^{10}C_8 \ 0.2{}^80.8^2 + {}^{10}C_7 \ 0.2{}^70.8^3 + {}^{10}C_6 \ 0.2{}^60.8^4 + {}^{10}C_5 \ 0.2{}^50.8^5 + {}^{10}C_4 \ 0.2{}^40.8^6 + {}^{10}C_3 \ 0.2{}^30.8^7]}{}$	M1	One term ${}^{10}C_x p^x (1-p)^{10-x}$, for $0 < x < 10, 0 < p < 1$
		A1	Correct expression, accept unsimplified
	0.678	B1	0.677
		4	
4(d)	$0.8^6 \times 0.2 + 0.8^7 \times 0.2 = 0.0524288 + 0.041943$	M1	$p^{l} \times (1-p) + p^{m} \times (1-p), l = 6, 7$ $m = l + 1, 0$
	0.0944	A1	0.09437 ≤ <i>p</i> ≤ 0.0944
		2	

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Question	Answer	Marks	Guidance
5(a)	$P(X < 6) = P(Z < \frac{6 - 5.2}{1.5}) = P(Z < 0.5333)$	M1	6, 5.2, 1.5 substituted into \pm standardisation formula, condone 1.5 ² , continuity correction ± 0.5
	0.703	A1	
		2	
5(b)	$z_1 = \frac{3-\mu}{\sigma} = -1.329$ $z_2 = \frac{8-\mu}{\sigma} = 0.878$	B1	$1.328 < z_1 \leq 1.329$ or $-1.329 \leq z_1 < -1.328$
	$z_2 = \frac{8-\mu}{\sigma} = 0.878$	B1	$0.877 < z_2 \leq 0.878$ or $-0.878 \leq z_2 < -0.877$
	Solve to find at least one unknown: $\frac{3-\mu}{\sigma} = -1.329$ $\frac{8-\mu}{\sigma} = 0.878$	M1	Use of the ± standardisation formula once with μ , σ , a <i>z</i> -value (not 0.8179, 0.7910, 0.5367, 0.5753, 0.19, 0.092 etc.) and 3 or 8, condone continuity correction but not σ^2 or $\sqrt{\sigma}$
	$\frac{1}{\sigma} = 0.878$	M1	Use either the elimination method or the substitution method to solve their two equations in μ and σ
	$\sigma = 2.27, \mu = 6.01$	A1	$2.26 \leqslant \sigma \leqslant 2.27, 6.01 \leqslant \mu \leqslant 6.02$
		5	

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Question	Answer	Marks	Guidance
5(c)	$[P(Z < -1) + P(Z > 1)] \Phi(1) - \Phi(-1) =$	M1	Identify 1 and -1 as the appropriate <i>z</i> -values.
	$= 2 - 2 \Phi(1) = 2 - 2 \times 0.8413$	M1	Calculating the appropriate area from stated phis of z -values which must be \pm the same number
	0.3174	A1	Accept AWRT 0.317
	Number of leaves: $2000 \times 0.3174 = 634.8$ so 634 or 635	B1 FT	FT <i>their</i> 4 s.f. (or better) probability, final answer must be positive integer no approximation or rounding stated
		4	

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	roblisheb						
Question	Answer	Marks	Guidance				
6(a)	$0.6 + 0.4 \times 0.3 = 0.72$ or $1 - 0.4 \ge 0.72 = 0.72$	B1	Clear identified calculation AG				
		1					
6(b)	$0.72 \times (0.4 + 0.6 \times 0.2)$	M1	$0.72 \times u, 0 < u < 1$				
		M1	$v \times (0.4 + 0.6 \times 0.2)$, or $v \times (1 - 0.6 \times 0.8) \ 0 < v \le 1$ no additional terms SC B1 for $0.72 \times (0.4 + 0.12)$ or $0.72 \times (1 - 0.48)$				
	0.3744	A1	WWW. Condone 0.374. SC B1 for 0.3744 only				
		3					
	Alternative method for question 6(b)						
	[p(P1P2) + p(F1P1P2) + p(P1F2P2) + p(F1P1F2P2)] =	M1	Any two terms unsimplified and correct				
	$0.6 \times 0.4 + 0.4 \times 0.3 \times 0.4 + 0.6 \times 0.6 \times 0.2 + 0.4 \times 0.3 \times 0.6 \times 0.2$		Summing 4 appropriate scenarios by listing or on a tree diagram SC B1 for 0.24 + 0.048 + 0.072 + 0.0144				
	0.3744	A1	WWW. Condone 0.374. SC B1 for 0.3744 only				
		3					

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Question	Answer	Marks	Guidance
6(c)	$P(\text{fails first or second level} \text{finishes game}) = \frac{P(\text{fails first or second level} \cap \text{finishes game})}{their(\mathbf{b})}$	M1	Either $0.6 \times 0.6 \times 0.2$ or $0.4 \times 0.3 \times 0.4$ seen Condone 0.072 or 0.048 if seen in (b)
	Numerator = P(S SF) + P(FS S) = $0.6 \times 0.6 \times 0.2 + 0.4 \times 0.3 \times 0.4 = 0.072 + 0.048 = 0.12$	A1	Both correct accept unsimplified expression. No additional terms
	Required probability = $\frac{0.12}{their(\mathbf{b})}$	M1	$\frac{Their \text{ sum of two 3-term probabilities as numerator}}{their (b) \text{ or correct}}$
	0.321 or $\frac{25}{78}$	A1	0.3205
		4	